Microeconomics HU WS 2006/2007, Exercises 3 (two pages)

Exercises for Chapter 5

- 13. Derive graphically an uncompensated demand curve for a Giffen-good from an indifference curve diagram.
- 14. A demand function takes the form $\mathbf{x} = \mathbf{p}_x^a \bullet \mathbf{p}_y^b \bullet \mathbf{I}^c$
 - a. What are the income and price elasticities of demand for x?
 - b. What relationship between parameters needs to hold in order to rule out money illusion?
 - c. If money illusion is ruled out, the same equation can be written as $x = (p_v/p_x)^d \cdot (I/p_x)^e$

What is the relationship between a, b and c on the one hand and d and e on the other hand?

- 15. Do rich households consume only luxuries?
- 16. What do you think about the following statement: Poor people can make only little use of additional income, because they spend a high share of their income on food products which have very low income elasticities.
- 17. Would you assume total demand for food in developing countries to be more or less price elastic than in industrialized countries? Why?
- 18. Which of the following combinations of signs (Vorzeichen) of uncompensated own price elasticity ($\mathcal{E}_{x, p}$), compensated own price elasticity ($\mathcal{E}_{x, p}$) and income elasticity ($\mathcal{E}_{x, I}$) of demand for X are possible? What kinds of goods are depicted?

	$\mathcal{E}_{\mathrm{x, p}}$	$\mathcal{E}^{c}_{x, p}$	$\mathcal{E}_{\mathrm{x,I}}$
1	+	+	+
2	-	+	+
3	+	-	+
4	-	-	+
5	-	-	-
6	+	-	-

- a. Derive the compensated demand curves for the utility function in exercise no. 11 on exercises sheet 2.
- b. Check whether the slope of the compensated demand curve derived in a is identical with the substitution effect which can be derived directly from the demand function calculated in exercise 11.c on sheet 2.
- 20. A consumer has the utility function $U = x_1^{0.006} \cdot x_2^{0.594}$ with x_1 being her consumption of beef and x_2 her consumption of all other goods. Her yearly income is \notin 40,000 per year and the price for beef is \notin 20 per kg. The price of x_2 is defined as \notin 1 per unit.
 - a. Derive the normal demand function for beef and calculate the quantity consumed.
 - b. Derive the compensated demand function and determine its slope.
 - c. Agricultural policy is liberalized and the beef prices falls to €10 per kg. calculate the change in "consumer cost" (the compensating variation) which results from this price change.
 - d. Compare the compensating variation calculated in c. to the following approximations of the welfare change resulting from the price reduction:
 - i. Assume that the compensated demand curve is linear and has the slope derived in b.
 - ii. Calculate the quantities of beef for the prices of €10 and €20 with the compensated demand curve and assume that the compensated demand curve is a linear between these points.
 - iii. Calculate the welfare change as the change in consumer surplus as an integral under the normal demand curve (hint: the integral of (1/x)dx is $\ln x$).

19.